

# Complete One-Loop Renormalization of the Higgs-Electroweak Chiral Lagrangian

— Chiral Dynamics 2018, Durham, NC —

Claudius Krause

Fermi National Accelerator Laboratory

September 17, 2018

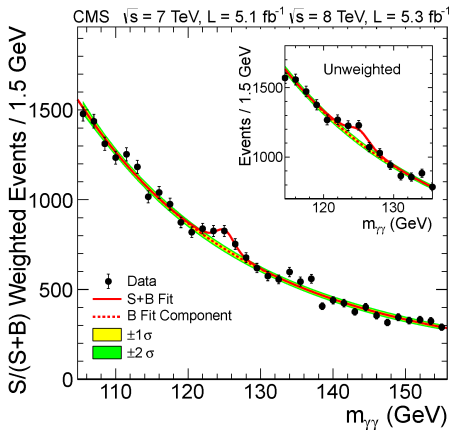
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In collaboration with:  
Gerhard Buchalla, Oscar Catà, Alejandro Celis, and Marc Knecht,  
arXiv:1710.06412, Nucl. Phys. B **928** (2018) 93

# Is that the Higgs of the Standard Model?



[1207.7235]

⇒ Answers beyond Yes/No are best addressed using a (model-independent) bottom-up Effective Field Theory.

# The interest in EFT techniques increased a lot, recently\*.

SMEFT: (weakly-coupled) new physics beyond the (complete) SM

- operator bases at dim 6, 7, ... Grzadkowski *et al.*; Lehman; Liao/Ma;...
- operator counting Henning/Lu/Melia/Murayama
- 1-loop renormalization Alonso/Jenkins/Manohar/Trott
- matching to models Henning *et al.*; Fuentes-Martin *et al.*
- tools: SMEFTsim, DsixTools, Rosetta Brivio *et al.*; Celis *et al.*;  
Falkowski *et al.*

EWCh $\mathcal{L}$  : (strongly-coupled) new physics in the Higgs sector

- operator basis Buchalla *et al.*; Alonso *et al.*
- relation between SMEFT and EWCh $\mathcal{L}$  Brivio *et al.*; Buchalla *et al.*
- geometric picture Alonso/Jenkins/Manohar
- renormalization of scalar sector Gavela *et al.*; Guo *et al.*;  
Alonso *et al.*

\* not meant to be a complete list

# Why is the complete 1-loop renormalization useful?

- to determine the divergence structure of the EWCh $\mathcal{L}$ 
  - ⇒ confirm power counting
  - ⇒ confirm operator basis
  - ⇒ get running of LO couplings

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- *“To learn something about Field Theory”*

Mike Trott, ca. 2013/14

⇒ have to tackle  $\infty$  Feynman diagrams

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## Abstract

Employing background-field method and super-heat-kernel expansion, we compute the complete one-loop renormalization of the electroweak chiral Lagrangian with a light Higgs boson. Earlier results from purely scalar fluctuations are confirmed as a special case. We also recover the one-loop renormalization of the conventional Standard Model in the appropriate limit.

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# I: ...of the electroweak chiral Lagrangian with a light Higgs.

The EWCh $\mathcal{L}$  is Chiral Perturbation Theory applied to Higgs physics.

Ingredients:

- Particles: all SM particles, but we do not assume a relation between the GB and the Higgs
- Symmetries:  $SU(3)_C \times SU(2)_L \times U(1)_Y \rightarrow SU(3)_C \times U(1)_{em}, B, L$   
at LO: flavor and custodial symmetry
- Power counting: in terms of chiral dimensions (generalized momenta)

$$2L + 2 = [\text{couplings}]_X + [\text{derivatives}]_X + [\text{fields}]_X$$

$$[\text{bosons}]_X = 0,$$

$$[\text{fermion bilinears}]_X = [\text{derivatives}]_X = [\text{weak couplings}]_X = 1$$

Buchalla/Catà/CK [1312.5624]



# I: ...of the electroweak chiral Lagrangian with a light Higgs.

$$\begin{aligned}\mathcal{L}_{\text{LO}} = & \frac{v^2}{4} \langle (D_\mu U)(D^\mu U^\dagger) \rangle (1 + F_U(h)) + \frac{1}{2}(\partial_\mu h)(\partial^\mu h) - \mathcal{V}(h) \\ & + i\bar{\Psi}_f \not{D} \Psi_f - (v \bar{\Psi}_f U Y_f(h) \Psi_f + \text{h.c.}) \\ & - \frac{1}{2} \langle G_{\mu\nu} G^{\mu\nu} \rangle - \frac{1}{2} \langle W_{\mu\nu} W^{\mu\nu} \rangle - \frac{1}{4} B_{\mu\nu} B^{\mu\nu}\end{aligned}$$

Feruglio[hep-ph/9301281], Bagger *et al.*[hep-ph/9306256], Chivukula *et al.*[hep-ph/9312317], Wang/Wang[hep-ph/0605104], Grinstein/Trott[0704.1505], Contino[1005.4269], Alonso *et al.*[1212.3305], Buchalla/Catà/CK [1307.5017], Buchalla/Catà/Celis/CK [1603.03062], ...

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$$+ i\bar{\Psi}_c \not{D}\Psi_c$$

In unitary gauge:

$$-\frac{v^2}{4} \langle (D_\mu U)(D^\mu U^\dagger) \rangle = \frac{g^2 v^2}{4} W_\mu^+ W^{\mu-} + \frac{(g^2 + g'^2)v^2}{8} Z_\mu Z^\mu$$

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## Properties:

- It has generalized Higgs-couplings compared to the SM.  
⇒ related to the  $\kappa$ -formalism at LO.
- There is a hierarchy to the operators that modify the EWPD.
- It captures the low-energy effects of strongly-coupled new physics.
- It is non-renormalizable at LO.

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Employing background-field method and super-heat-kernel expansion, we compute the complete one-loop renormalization of the electroweak chiral Lagrangian with a light Higgs boson. Earlier results from purely scalar fluctuations are confirmed as a special case. We also recover the one-loop renormalization of the conventional Standard Model in the appropriate limit.

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arXiv:1710.06412, Nucl. Phys. B **928** (2018) 93



## II.1: Employing Background-Field Method and ...

starting from the generating functional:

$$Z[j, \rho, \bar{\rho}] = e^{iW[j, \rho, \bar{\rho}]} = \int [d\phi d\psi d\bar{\psi}] e^{i(S[\phi, \psi, \bar{\psi}] + j\phi + \bar{\psi}\rho + \bar{\rho}\psi)},$$

$$\phi = \hat{\phi} + \phi_{qu}, \quad \psi = \hat{\psi} + \psi_{qu},$$

$$\Rightarrow e^{iW_{L=1}} = \int [d\phi_{qu} d\psi_{qu} d\bar{\psi}_{qu}] e^{iS^{(2)}[\hat{\phi}, \hat{\psi}, \hat{\bar{\psi}}; \phi_{qu}, \psi_{qu}, \bar{\psi}_{qu}]}$$

Abbott '81

Quantum gauge fixing:

$$\mathcal{L}_{\text{gauge-fix}} = -\frac{1}{2\xi} \left( \partial_\mu B^\mu + \frac{\xi}{2} g' v \varphi_3 \right)^2 - \frac{1}{\xi} \text{Tr} \left\{ \left( \hat{D}_W^\mu W_\mu - \frac{\xi}{2} g v \hat{U}_\varphi \hat{U}^\dagger \right)^2 \right\}$$

- The terms proportional to  $\varphi$  will make the next steps easier.
- Later, we will set  $\xi = 1$ .

Dittmaier/Grosse-Knetter hep-ph/9505266

## II.2: ... and Super-Heat-Kernel Expansion, we compute ...

evaluating the one-loop functional

Neufeld/Gasser/Ecker hep-ph/9806436

$$e^{iW_{L=1}} = \int [d\phi d\psi d\bar{\psi}] e^{iS^{(2)}[\hat{\phi}, \hat{\psi}, \hat{\bar{\psi}}; \phi, \psi, \bar{\psi}]}$$

$$S^{(2)} = \frac{1}{2} \phi A \phi + \bar{\psi} B \psi + \phi \bar{\Gamma} \psi + \bar{\psi} \Gamma \phi$$

$$W_{L=1} = \frac{i}{2} \text{Tr} \ln A - i \text{Tr} \ln B - \frac{i}{2} \sum_{n=0}^{\infty} \frac{1}{n} \text{Tr} (A^{-1} \bar{\Gamma} B^{-1} \Gamma - A^{-1} \Gamma^T B^{-1, T} \bar{\Gamma}^T)^n$$

## II.2: ... and Super-Heat-Kernel Expansion, we compute ...

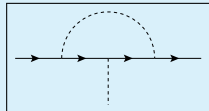
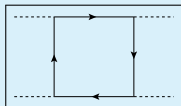
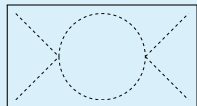
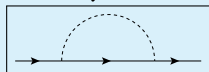
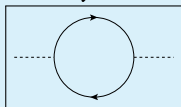
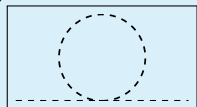
evaluating the one-loop functional

Neufeld/Gasser/Ecker hep-ph/9806436

$$e^{iW_{L=1}} = \int [d\phi d\psi d\bar{\psi}] e^{iS^{(2)}[\hat{\phi}, \hat{\psi}, \hat{\bar{\psi}}; \phi, \psi, \bar{\psi}]}$$

$$S^{(2)} = \frac{1}{2} \phi A \phi + \bar{\psi} B \psi + \phi \bar{\Gamma} \psi + \bar{\psi} \Gamma \phi$$

$$W_{L=1} = \frac{i}{2} \text{Tr} \ln A - i \text{Tr} \ln B - \frac{i}{2} \sum_{n=0}^{\infty} \frac{1}{n} \text{Tr} (A^{-1} \bar{\Gamma} B^{-1} \Gamma - A^{-1} \Gamma^T B^{-1, T} \bar{\Gamma}^T)^n$$



## II.2: ... and Super-Heat-Kernel Expansion, we compute ...

Introducing supermatrix algebra:

Neufeld/Gasser/Ecker hep-ph/9806436

$$M = \begin{pmatrix} a & b \\ c & d \end{pmatrix}$$

$$\text{Sdet } M = \det(a - bd^{-1}c) \det d^{-1}$$

$$\text{Str } M = \text{Tr } a - \text{Tr } d$$

$$\text{Sdet } M = e^{\text{Str } \ln M}$$

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$$\text{Sdet } M = e^{\text{Str } \ln M}$$

The one-loop functional becomes:

$$W_{L=1} = \frac{i}{2} \text{Str } \ln K,$$

$$K = \begin{pmatrix} A & \bar{\Gamma} & -\Gamma^T \\ -\bar{\Gamma}^T & 0 & -B^T \\ \Gamma & B & 0 \end{pmatrix}$$

## II.2: ... and Super-Heat-Kernel Expansion, we compute ...

The Heat-Kernel Expansion extracts the  $\frac{1}{\epsilon}$ -poles of  $W_{L=1}$ .

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With

Donoghue/Golowich/Holstein '92; Neufeld/Gasser/Ecker hep-ph/9806436

$$K = (\partial_\mu + \Lambda_\mu)(\partial^\mu + \Lambda^\mu) + \Sigma$$

we get

$$W_{L=1,div} = \frac{1}{32\pi^2\epsilon} \int d^4x \operatorname{str} \left[ \frac{1}{12} \Lambda_{\mu\nu} \Lambda^{\mu\nu} + \frac{1}{2} \Sigma \Sigma \right].$$

$$\Lambda_{\mu\nu} = \partial_\mu \Lambda_\nu - \partial_\nu \Lambda_\mu + [\Lambda_\mu, \Lambda_\nu]$$

- Specifying the Dirac structure of  $S^{(2)}$ , we can further evaluate the Dirac-traces.
- The resulting Master-Formula is purely algebraic (Matrix multiplication and traces).

'tHooft '73

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## Abstract

Employing background-field method and super-heat-kernel expansion, we compute the complete one-loop renormalization of the electroweak chiral Lagrangian with a light Higgs boson. Earlier results from purely scalar fluctuations are confirmed as a special case. We also recover the one-loop renormalization of the conventional Standard Model in the appropriate limit.

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### III: ... the Complete One-Loop Renormalization of the ...

#### Cross-checks:

- We reproduce previous results of the Scalar sector.  
Guo/Ruiz-Femenía/Sanz-Cillero, Phys. Rev. D **92** (2015) 074005, arXiv:1506.04204
- We reproduce the SM- $\beta$ -functions in the SM-limit.
- We performed 5 independent computations with 2 different choices of  $\mathcal{L}_{\text{gauge-fix}}$ .

### III: ... the Complete One-Loop Renormalization of the ...

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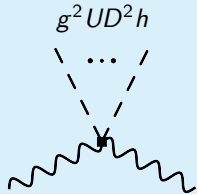
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- We performed 5 independent computations with 2 different choices of  $\mathcal{L}_{\text{gauge-fix}}$ .

#### The result:

see also Alonso *et al.*, arXiv:1710.06848, PRD

- confirms the predictions by power counting.  
Buchalla/Catà/CK, Phys. Lett. B **731** (2014) 80, arXiv:1312.5624
- is consistent with the operator basis.  
Buchalla/Catà/CK, Nucl. Phys. B **880** (2014) 552, arXiv:1307.5017

### III: ... the Complete One-Loop Renormalization of the ...



$$\mathcal{O}_\beta = (g'v)^2 \langle UT_3 D_\mu U^\dagger \rangle^2 \mathcal{F},$$

1/1 operator,  $\sim (F_U - F_U^2/4)$



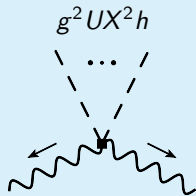
$$\mathcal{O}_{D1} = \langle D_\mu UD^\mu U^\dagger \rangle^2 \mathcal{F},$$

5/15 operators generated



$$\mathcal{O}_{XU7} = g' \langle T_3 D_\mu U^\dagger D_\nu U \rangle B^{\mu\nu} \bar{\mathcal{F}},$$

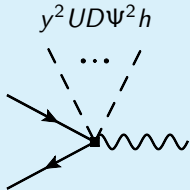
0/8 operators generated



$$\mathcal{O}_{Xh1} = g'^2 B_{\mu\nu} B^{\mu\nu} \bar{\mathcal{F}},$$

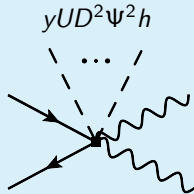
0/10 operators, (3 op.  $\mathcal{F}(h) = \text{const.} \Rightarrow \mathcal{L}_{LO}$ )

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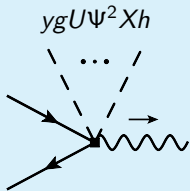
$$\mathcal{O}_{\Psi V1} = iy^2(\bar{q}_L\gamma^\mu q_L)\langle UT_3 D_\mu U^\dagger \rangle \mathcal{F},$$

13/13 operators generated



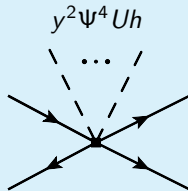
$$\mathcal{O}_{\Psi S1/2} = y\bar{q}_L U P_\pm q_R \langle D_\mu U D^\mu U^\dagger \rangle \mathcal{F},$$

12/30 operators generated (+h.c.)



$$\mathcal{O}_{\Psi X1/2} = yg'\bar{q}_L\sigma_{\mu\nu} U P_\pm q_R B^{\mu\nu} \mathcal{F},$$

0/11 operators generated (+h.c.)



$$\mathcal{O}_{LL1} = y^2(\bar{q}_L\gamma^\mu q_L)(\bar{q}_L\gamma_\mu q_L) \mathcal{F},$$

22/60 operators (+h.c.), from  $Y \cdot Y$  or  $Y^a \cdot Y^a$

# Summary

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The Super-Heat-Kernel Expansion gives a universal Master-Formula: Extracting the UV-divergencies is now reduced to matrix multiplication and tracing.

The result is consistent with the operator basis and confirms the power counting. It reproduces the Scalar divergencies and the SM- $\beta$ -functions in the appropriate limits.